## Concepts on Test \#4

## Simplifying algebraic expressions

EX. Simplify $7(x+3)+4 x^{2}+5 x-12-2\left(x^{2}+3 x\right)$

## Adding/subtracting polynomials

EX. Subtract $\left(3 \mathrm{x}-5 \mathrm{x}^{2}+9\right)-\left(4-17 \mathrm{x}^{2}+4 \mathrm{x}\right)$

## Multiplying polynomials

Product Rule for Exponents: $a^{r} \cdot a^{s}=a^{r+s}$
Mono x Mono:
EX. Simplify $\left(5 x^{2} y^{3}\right)\left(2 x^{3} y^{8}\right)$
Mono x Polynomial:
EX. Simplify $2 x^{2}\left(3 x^{3}+2 x-5\right)$
Binomial x Binomial:
EX. Simplify/Multiply $(2 x+5)(3 x-9)$
Special Case: Conjugates Multiplied
EX. Multiply $(2 \mathrm{x}+4)(2 \mathrm{x}-4)$
Associative Prop used
Mono x Binomial x Binomial:
EX. Multiply $2 \mathrm{x}(3 \mathrm{x}+5)(3 \mathrm{x}+4)$
Binomial x Polynomial:
EX. Multiply/Simplify $(2 x+1)\left(3 x^{2}+2 x+5\right)$

## Solving Algebraic Equations

Simplifying $1^{\text {st }}$
Combine like terms only:

$$
\text { EX. Solve a) } 2 x=3 x-10+4 x \quad \text { b) } 5 x-7+12=10
$$

Distributive prop \& combining:
EX. Solve a) $2(x+3)+5=9 \quad$ b) $3(x+4)-2 x=-44$
Using the addition prop more than once:
EX. Solve $2 x+5=9 x-2$
Using the multiplication prop after addition prop \& simplification:
EX. Solve $2 \mathrm{x}+9=5 \mathrm{x}+7-84$
Checking as substitution:
Check your answer to
EX. Solve a) $2 \mathrm{x}=3 \mathrm{x}-10+4 \mathrm{x}$
b) $3(x+4)-2 x=-44$

Prime Numbers vs Composite
Prime factorization
Using exponential notation
EX. Find prime factorization for $108 \& 96$ writing as a product of primes
ALL factors of a number:
EX. List all the factors of $108 \& 96$

## Greatest Common Factor

For \# via ALL factors:
EX. Find the GCF of 108 \& 96
For variables-- lowest exponent:
EX. Find the GCF of $x^{2} y^{3} z, x^{3} y^{2} z^{2} \& x^{5} y^{3}$
Monomial / Monomial:
Quotient Rule: $a^{r} \div a^{s}=a^{r-s}$
EX. Divide $15 x^{3} y^{7} \div 45 x^{2} y^{3}$
Factoring a Polynomial w/ GCF:
Find GCF
Rewrite as GCF (sum of quotients of original by GCF)
EX. Factor $12 \mathrm{x}^{3}+3 \mathrm{x}^{2}+9 \mathrm{x}$

## Fractions

Visual interpretation of fractions:
Proper Fractions
Improper Fractions
Mixed \#'s:
EX. Draw a picture to represent a) $2 / 3$ b) $13 / 4$ c) $9 / 5$

## Reducing Fractions:

With Prime factors
Cancel
GCF Method
Rewrite as product \& cancel OR divide out GCF
EX. Reduce/Put in lowest terms
a) $24 / 36$
b) $2^{15} / 18$

Finding LCD w/ primes
EX. Find the LCD of $\quad$ a) $28 \& 36$ b) $8 \& 10$
Mixed Numbers $<==>$ Improper Fractions
EX. Change $23 / 5$ to an improper fraction
EX. Change ${ }^{17} / 5$ to a mixed number
Adding Fractions w/ Common Denominators
Add numerators \& carry along denominator
EX. Add $\quad 7 / 48+12 / 48$
Reducing if needed (see above)
EX. Add $\quad 36 / 48+2 / 48$

