

# Example 1 Ellipses p. 7 Ch 11

This is an shifted ellipse

We began this problem in Example a)

$$9x^2 - 36x + 4y^2 = 0$$

- Starting from where we left off in Example #a on page 7

$$\frac{(x - 2)^2}{4} + \frac{y^2}{9} = 1$$

$$\frac{(x-2)^2}{4} + \frac{y^2}{9} = 1$$

- Get a, b & c
- $a^2$  is the larger denominator  
so,  $a^2 = 9$       so,  $a = 3$
- $b^2$  is the smaller denominator  
so,  $b^2 = 4$       so,  $b = 2$
- $c^2 = a^2 - b^2$   
so,  $c = \sqrt{c^2} = \pm\sqrt{9 - 4} = \pm\sqrt{5}$   
so,  $c = \approx\pm 2.2$

## a) Give the center

- The center is at (h, k)

$$\frac{(x - 2)^2}{4} + \frac{y^2}{9} = 1$$

So,

$$C(2, 0)$$

## b) Find the Foci

- Use  $c$  to give the foci. For an ellipse which a vertical major axis ( $y^2$  denominator  $>$   $x^2$  denominator) the foci will be  $(h, k + c)$  &  $(h, k - c)$

$$F_1(2, 0 + 3) \quad \& \quad F_2(2, 0 - 3)$$

So,  $F_1(2, 3)$  &  $F_2(2, -3)$

## c) Give the Vertices

- The vertices are  $(h, k + a)$  &  $(h, k - a)$  since this ellipse has a major axis that is vertical

$$V_1(2, 0 + 3) \text{ \& } V_2(2, 0 - 3)$$

So,  $V_1(2, 3)$  &  $V_2(2, -3)$

## d) Find the Eccentricity

- The eccentricity tells us how “squashed” the ellipse is around its major axis.  $e = c/a$

So,  $e = \sqrt{5}/3$

*Note: This is looking less like a circle because it is closer to 1 than it is to zero.*

## e) Find the Major Axis length

- The major axis is vertical since the larger denominator is on the  $y^2$ . That is  $a^2$  &  $a = 3$

$$\text{Major Axis Length: } 2(3) = 6$$

So, we see that the vertices being at  $(2, 3)$  &  $(2, -3)$  puts them 6 units apart which is the length of the major axis.



## f) Find the Minor Axis length

- The minor axis is horizontal since the smaller denominator is on the  $x^2$ . That is  $b^2$  &  $b = 2$

$$\text{Minor Axis Length: } 2(2) = 4$$

So, we see that two points on a horizontal line through the center, and 2 units to the left & right of center are at  $(2-2, 0)$  &  $(2+2, 0)$  or  $(0, 0)$  &  $(4, 0)$  putting them 4 units apart which is the length of the minor axis.

## g) Sketch the graph

- 1<sup>st</sup> Place the vertices
- 2<sup>nd</sup> Place the foci
- 3<sup>rd</sup> Place the 2 points on the minor axis
- 4<sup>th</sup> Draw the ellipse

